

Overview of Statistics 572

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Welcome to Statistics 572!

- Introduction
 - Bret Larget
- Comment on syllabus.
 - Textbook (better written than last year's choice)
 - Web for notes and grades (print notes before lecture)
 - Objectives
 - Computing (go R!)
 - Assignments (late policy)
 - Exams (save dates)
 - Grading
 - Academic honesty
 - Discussion sections (attend the one you want)

Some Changes from Last Year

- The textbook is better written, so I can count on you to learn through reading more than in the past. **I will not try to cover every topic in lecture.**
- Instead of attempting to blend some new ideas into the structure of what other instructors have done with 572 in the past, I am (mostly) going to cover what I want to and will not cover some topics that used to be in the course. I will stay pretty close to the textbook.
- I will attempt to incorporate some more active learning opportunities in class.
- I want you to become adept in R so I will spend more time on it in class and will ask you to do more with it on homework.

The Big Picture

- A statistical approach to data analysis can lend *insight to biological understanding* of a wide variety of problems.
- In a statistical approach, measurable variables are treated *as realizations from a model* that relates biological meaningful parameters and stochastic sources of variation.
- No model accounts for all aspects of the underlying biology, but *an appropriately selected model can be very useful.*
- Many data analysis problems arising from the biological sciences *are appropriate for linear and generalized linear models*, a rich family of possible models.

Variables

- Typically, one variable of interest is modeled as a *response variable* which is related to one or more *explanatory variables*.
- Variables can be categorized as *quantitative* or *categorical*.
- Quantitative variables are typically either measured on a *continuous scale* or are *discrete*, variables that are *counts*.
- The appropriate choice of model is determined in part by the *types of the response and explanatory variables*.
- A *linear combination* of the variables X_1, \dots, X_k takes the form

$$\beta_1 X_1 + \beta_2 X_2 + \dots + \beta_k X_k$$

- Linear and generalized linear models include *linear combinations of explanatory variables*.

Examples of Linear Models

- *Simple Linear Regression.*—
 response variable: continuous quantitative variable
 explanatory variable: one quantitative variable
 error structure: normal distribution
 model: $y_i = \beta_0 + \beta_1 x_i + e_i, \quad e_i \sim N(0, \sigma^2)$
 example: response variable is phosphorous concentration in plant tissue, explanatory variable is phosphorous concentration in the soil.
- *Multiple Linear Regression.*—
 response variable: continuous quantitative variable
 explanatory variables: more than one quantitative variables
 error structure: normal distribution
 model: $y_i = \beta_0 + \beta_1 x_{1i} + \dots + \beta_k x_{ki} + e_i, \quad e_i \sim N(0, \sigma^2)$
 example: response variable is soybean yield, explanatory variables are hours of daylight and amount of nitrogen.

Examples of Linear Models (cont.)

- *One-way ANOVA.*—
 response variable: continuous quantitative variable
 explanatory variable: one categorical variable
 error structure: normal distribution
 model: $y_{ij} = \alpha_i + e_{ij}, \quad e_{ij} \sim N(0, \sigma^2)$
 example: response variable is milk yield explanatory variable is diet (four treatments)
- *Multi-way ANOVA.*—
 response variable: continuous quantitative variable
 explanatory variables: more than one categorical variables
 error structure: normal distribution
 model: $y_{ijk} = \alpha_i + \beta_j + (\alpha\beta)_{ij} + e_{ijk}, \quad e_{ijk} \sim N(0, \sigma^2)$
 example: response variable nitrogen level in manure, explanatory variables are diet treatment, period, and interaction.

Examples of Linear Models (cont.)

- *Linear models with both types.*—
 response variable: continuous quantitative variable
 explanatory variables: both quantitative and categorical
 error structure: normal distribution
 model: $y_{ij} = \beta_0 + \beta_1 x_{ij} + \alpha_i + e_{ij}, \quad e_{ij} \sim N(0, \sigma^2)$
 example: response variable is milk yield, explanatory variables are diet (four treatments) and days in milk.
- *Polynomial regression.*—
 response variable: continuous quantitative variable
 explanatory variables: single quantitative explanatory variable
 error structure: normal distribution
 model: $y_i = \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \beta_3 x_i^3 + e_i, \quad e_i \sim N(0, \sigma^2)$
 example: response variable is disease area, explanatory variable is age

Examples of Linear Models (cont.)

- *Mixed models.*—

response variable: continuous quantitative variable

explanatory variables: variables of both *fixed* and *random* effect.

error structure: normal distribution

model: $y_{ij} = \beta_0 + \beta_1 x_{ij} + a_i + e_{ij}$, $e_{ij} \sim N(0, \sigma^2)$, $a_i \sim N(0, \sigma_a^2)$

example: response variable is percentage cover of vegetation, site is modeled as a random effect, quantitative variables include soil moisture.

- *Repeated measures.*—

response variable: continuous quantitative variable

explanatory variables: one or more including random effect for individual

error structure: normal distribution

example: response variable is hormone concentration, explanatory variables include individual and day.

Examples of Generalized Linear Models

- *Logistic Regression.*—

response variable: categorical variable with two levels

explanatory variables: one or more

error structure: binomial

model: $P\{y_i = 1\}$ is a function of $\beta_0 + \beta_1 x_{1i} + \beta_2 x_{2i}$.

example: response variable is seed germination, explanatory variables include temperature and treatment.

- *Poisson regression.*—

response variable: non-negative integer-valued variable

explanatory variables: one or more

error structure: Poisson

model: $P\{y_i = k\}$ is a function of $\beta_0 + \beta_1 x_{1i} + \beta_2 x_{2i}$.

example: response variable is number of seeds produced, explanatory variables include treatment and light intensity.

Data request

- I will present each type of model with an example and data.
- These case studies will be more interesting if they are related to *genuine research problems*.
- If you or someone in your lab *has data that falls into the scope of these models*, and you are willing/able to share, *please contact me*.