Welcome to Statistics 572!

- Introduce self and TAs.
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- Comment on syllabus.
  - Textbook
  - Web for notes and grades (print notes before lecture)
  - Objectives
  - Computing (go R!)
  - Assignments (late policy)
  - Exams (save dates)
  - Grading
  - Academic honesty
  - Discussion sections (attend the one you want)
The Big Picture

- A statistical approach to data analysis can lend *insight to biological understanding* of a wide variety of problems.
- In a statistical approach, measurable variables are treated *as realizations from a model* that relates biological meaningful parameters and stochastic sources of variation.
- No model accounts for all aspects of the underlying biology, but *an appropriately selected model can be very useful*.
- Many data analysis problems arising from the biological sciences *are appropriate for linear and generalized linear models*, a rich family of possible models.

Variables

- Typically, one variable of interest is modeled as a *response variable* which is related to one or more *explanatory variables*.
- Variables can be categorized as *quantitative or categorical*.
- Quantitative variables are typically either measured on a *continuous scale* or are *discrete*, variables that are *counts*.
- The appropriate choice of model is determined in part by the *types of the response and explanatory variables*.
- A *linear combination* of the variables $X_1, \ldots, X_k$ takes the form
  \[ \beta_1 X_1 + \beta_2 X_2 + \cdots + \beta_k X_k \]
- Linear and generalized linear models include *linear combinations of explanatory variables*. 
Examples of Linear Models

- **Simple Linear Regression.**
  - response variable: continuous quantitative variable
  - explanatory variable: one quantitative variable
  - error structure: normal distribution
  - model: \( y_i = \beta_0 + \beta_1 x_i + e_i, \quad e_i \sim N(0, \sigma^2) \)
  - example: response variable is phosphorous concentration in plant tissue, explanatory variable is phosphorous concentration in the soil.

- **Multiple Linear Regression.**
  - response variable: continuous quantitative variable
  - explanatory variables: more than one quantitative variables
  - error structure: normal distribution
  - model: \( y_i = \beta_0 + \beta_1 x_{1i} + \cdots + \beta_k x_{ki} + e_i, \quad e_i \sim N(0, \sigma^2) \)
  - example: response variable is soybean yield, explanatory variables are hours of daylight and amount of nitrogen.

Examples of Linear Models (cont.)

- **One-way ANOVA.**
  - response variable: continuous quantitative variable
  - explanatory variable: one categorical variable
  - error structure: normal distribution
  - model: \( y_{ij} = \alpha_i + e_{ij}, \quad e_{ij} \sim N(0, \sigma^2) \)
  - example: response variable is milk yield explanatory variable is diet (four treatments)

- **Multi-way ANOVA.**
  - response variable: continuous quantitative variable
  - explanatory variables: more than one categorical variables
  - error structure: normal distribution
  - model: \( y_{ijk} = \alpha_i + \beta_j + (\alpha \beta)_{ij} + e_{ijk}, \quad e_{ijk} \sim N(0, \sigma^2) \)
  - example: response variable nitrogen level in manure, explanatory variables are diet treatment, period, and interaction.
Examples of Linear Models (cont.)

- **Linear models with both types.**
  - response variable: continuous quantitative variable
  - explanatory variables: both quantitative and categorical
  - error structure: normal distribution
  - model: \( y_{ij} = \beta_0 + \beta_1 x_{ij} + \alpha_i + e_{ij}, \quad e_{ij} \sim N(0, \sigma^2) \)
  - example: response variable is milk yield, explanatory variables are diet (four treatments) and days in milk.

- **Polynomial regression.**
  - response variable: continuous quantitative variable
  - explanatory variables: single quantitative explanatory variable
  - error structure: normal distribution
  - model: \( y_i = \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \beta_3 x_i^3 + e_i, \quad e_i \sim N(0, \sigma^2) \)
  - example: response variable is disease area, explanatory variable is age

- **Mixed models.**
  - response variable: continuous quantitative variable
  - explanatory variables: variables of both fixed and random effect.
  - error structure: normal distribution
  - model: \( y_{ij} = \beta_0 + \beta_1 x_{ij} + a_i + e_{ij}, \quad e_{ij} \sim N(0, \sigma^2), \quad a_i \sim N(0, \sigma_a^2) \)
  - example: response variable is percentage cover of vegetation, site is modeled as a random effect, quantitative variables include soil moisture.

- **Repeated measures.**
  - response variable: continuous quantitative variable
  - explanatory variables: one or more including random effect for individual
  - error structure: normal distribution
  - example: response variable is hormone concentration, explanatory variables include individual and day.
Examples of Generalized Linear Models

- **Logistic Regression.**—
  - response variable: categorical variable with two levels
  - explanatory variables: one or more
  - error structure: binomial
    - model: \( P \{ y_i = 1 \} \) is a function of \( \beta_0 + \beta_1 x_{1i} + \beta_2 x_{2i} \).
  - example: response variable is seed germination, explanatory variables include temperature and treatment.

- **Poisson regression.**—
  - response variable: non-negative integer-valued variable
  - explanatory variables: one or more
  - error structure: Poisson
    - model: \( P \{ y_i = k \} \) is a function of \( \beta_0 + \beta_1 x_{1i} + \beta_2 x_{2i} \).
  - example: response variable is number of seeds produced, explanatory variables include treatment and light intensity.

Data request

- I will present each type of model with an example and data.
- These case studies will be more interesting if they are related to genuine research problems.
- If you or someone in your lab has data that falls into the scope of these models, and you are willing/able to share, please contact me.